## Col•loqui

## Complex Brunn-Minkowski theorems

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The classical Brunn-Minkowski theorem is an inequality for volumes of convex bodies. It says that if $A$ and $B$ are convex bodies in $\mathbb{R}^{n}$ then their Minkowski sum

$$
A+B:=\{a+b ; a \in A, b \in B\}
$$

satisfies the inequality

$$
\operatorname{Vol}(A+B)^{1 / n} \geq \operatorname{Vol}(A)^{1 / n}+\operatorname{Vol}(B)^{1 / n}
$$

It has many applications and is particularly powerful since in some ways it goes in the opposite direction to simpler convexity statements like Hölder's inequality.

Its complex counterpart is a similar statement for $L^{2}$-norms of holomorphic functions (or forms, or sections of line bundles) on domains in $\mathbb{C}^{n}$ or complex manifolds. The complex version contains the real version as a special case, but is considerably more general. I will explain how this works and, time permitting, also indicate a few applications in algebraic and Kähler geometry.

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